

Forces - More Practice

Section 1 - \vec{F}_g

1.) Calculate the force of gravity on a 25 kg mass at the surface of the earth.

$$\vec{F}_g = m \times \vec{g} \quad \leftarrow \text{SAME AS } \vec{F} = m\vec{a}$$

$$\vec{F}_g = (25)(-9.81) \quad \boxed{\vec{F}_g = -245 \text{ N}}$$

2.) A 75 kg mass is on the surface of Mars when an astronaut lifts it with a spring scale. The scale has a reading of 259 N. What is the gravitational field strength on Mars?

$$\vec{F}_g = m \times \vec{g} \quad \frac{-259}{75} = \frac{75(\vec{g})}{75} \quad \vec{g} = -3.45 \text{ m/s}^2 \Rightarrow \boxed{-3.45 \text{ N} \times \text{kg}}$$

3.) How much force must a horizontal surface exert to hold up a 2.0 kg book and what is the name of that force? \vec{F}_n

$$\vec{w} = m \vec{g} \quad \vec{w} = (2.0)(-9.81)$$

$$\vec{w} = -19.6 \text{ N} \quad \therefore \vec{F}_n = +19.6 \text{ N}$$

Section 2 - \vec{F}_{net}

1.) A cat is dragged at a constant velocity of $+3.0 \frac{\text{m}}{\text{s}}$ across sandpaper. What is the total force on the cat?

$$\boxed{0 \text{ N}} \quad \begin{array}{l} \uparrow \\ \text{- NEWTON'S FIRST LAW} \\ \text{- ALL FORCES IN BALANCE} \end{array}$$

2.) A 1200 kg car is pushed by three students from rest to $+5.0 \frac{\text{m}}{\text{s}}$, 30 m along a level surface. What was the unbalanced force used on the car? (2)

$$\vec{F}_{net} = m \vec{a} \quad \vec{F}_{net} = (1200)(0.4166)$$

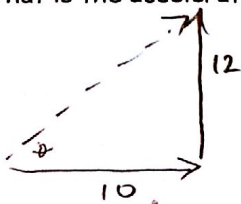
$$\boxed{\vec{F}_{net} = 500 \text{ N}}$$

(1) $\vec{v}_f^2 = \vec{v}_0^2 + 2\vec{a}d$
 $(+5.0)^2 = 0 + 2(\vec{a})(+30)$
 $\vec{a} = +0.4166 \text{ m/s}^2$

3.) Assuming the force of friction on the car in problem 2 was 100 N how much combined force did the students have to exert?



4.) What is the acceleration of a 5.0 kg mass when pulled with 10 N [E] and 12 N [N]?



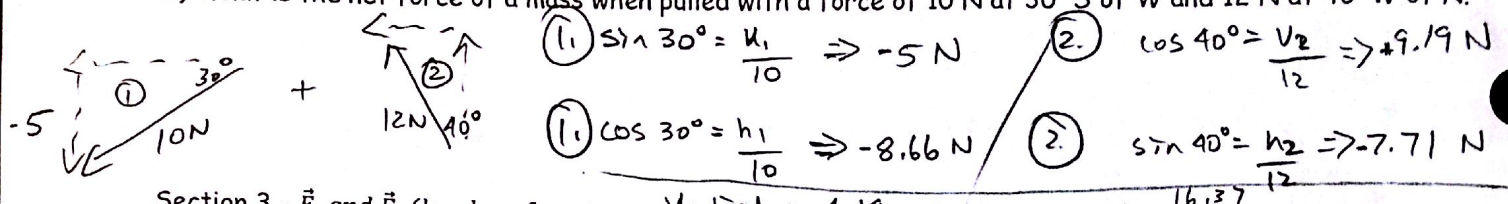
$$10^2 + 12^2 = h^2 \quad h = 15.6 \text{ N} \quad \vec{F}_{net} = m \vec{a}$$

$$\theta \Rightarrow \tan \theta = \frac{12}{10} \quad +15.6 = (5.0)(\vec{a})$$

$$\theta = 50.1944^\circ \quad \vec{a} = 3.12 \text{ m/s}^2$$

$$\boxed{3.12 \text{ m/s}^2 \text{ at } 50.2^\circ \text{ N of E}}$$

5.) What is the net force of a mass when pulled with a force of 10 N at 30° S of W and 12 N at 40° W of N.



(1) $\sin 30^\circ = \frac{v_1}{10} \Rightarrow -5 \text{ N}$

(2) $\cos 40^\circ = \frac{v_2}{12} \Rightarrow +9.19 \text{ N}$

(1) $\cos 30^\circ = \frac{h_1}{10} \Rightarrow -8.66 \text{ N}$

(2) $\sin 40^\circ = \frac{h_2}{12} \Rightarrow -7.71 \text{ N}$

Section 3 - \vec{F}_f and \vec{F}_n (level surfaces)

1.) A 10 kg mass is pulled along a level surface using a force of 25 N. What is the coefficient of friction?

$\vec{F}_f = \mu \vec{F}_n$

$-25 = \mu (+98.1)$

$\mu = 0.255$

2.) A force of 7.5 N is used to pull a rubber friction block across a table at constant speed. If the coefficient of friction is 0.35 what is the mass of the block?

(1) $\vec{F}_f = \mu \vec{F}_n$

$(-7.5) = (0.35)(\vec{F}_n)$

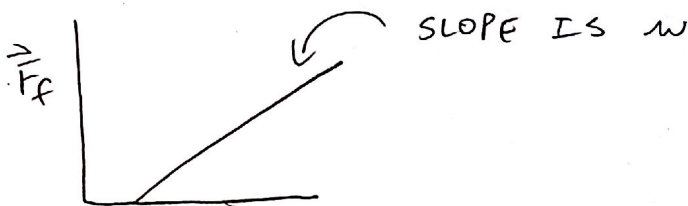
$\vec{F}_n = +21.42875 \text{ N}$

(2) $\vec{W} = m\vec{g}$

$-21.42875 = m(-9.81)$

$m = 2.18 \text{ kg}$

3.) What shape is a graph of \vec{F}_f vs. \vec{F}_n and what is the slope?



Section 4 - \vec{F}_e \vec{F}_n

1.) Calculate the extension of a spring whose spring constant is $20 \frac{\text{N}}{\text{m}}$ when a 0.50 kg mass is hung on it.

(1) $\vec{F}_e = \vec{W}$

$\vec{W} = m\vec{g}$

$\vec{W} = (0.50)(-9.81)$

$\vec{W} = -4.905$

(2) $\vec{F}_e = kx$

$4.905 = (20)(x)$

$x = 0.245 \text{ m}$

2.) What is the spring constant of a desk if a force of 784 N compresses it from height 1.00 m to 0.92 m?

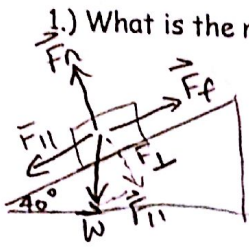
$\vec{F}_c = kx$

$-784 = k(0.08)$

$k = -9800 \frac{\text{N}}{\text{m}}$

Section 5: Forces on Ramps

(1) $\vec{w} = m \vec{g}$
 $\vec{w} = (5.0)(-9.8)$

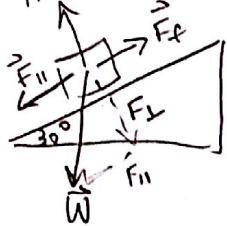


(2) $\vec{F}_n = \vec{F}_\perp$ / $F_\perp \Rightarrow \cos 40^\circ = \frac{F_\perp}{W}$

$\cos 40^\circ = \frac{F_\perp}{49.05}$ $\vec{F}_\perp = +37.6 \text{ N}$

(3) $\vec{F}_{||} \Rightarrow \sin 40^\circ = \frac{\vec{F}_{||}}{49.05}$ $\vec{F}_{||} = -31.5 \text{ N}$

2.) What is the acceleration of a 3.0 kg mass on a 30° frictionless-slope?



(2) $\vec{F}_{||} \Rightarrow \sin 30^\circ = \frac{\vec{F}_{||}}{-29.43}$
 $\vec{F}_{||} = -14.715 \text{ N}$

(1) $\vec{w} = m \vec{g}$ $\vec{w} = (3.0)(-9.8)$
 $\vec{w} = -29.43 \text{ N}$

(3) $\vec{F}_{net} = m \vec{a}$ $-14.7 = (3.0)(\vec{a})$ $\vec{a} = -4.9 \text{ m/s}^2$

3.) What is the normal force on the mass in #2 above?

$\vec{F}_n = \vec{F}_\perp$ $\vec{F}_\perp \Rightarrow \cos 30^\circ = \frac{\vec{F}_\perp}{-29.43}$ $\vec{F}_\perp \Rightarrow \cos 30^\circ = \frac{\vec{F}_\perp}{-29.43}$

$\vec{F}_\perp = +25.5 \text{ N}$

4.) What is the force of friction on the mass in #3 above if $\mu = 0.2$?

$\vec{F}_f = \mu \vec{F}_n$ $\vec{F}_f = (0.2)(25.487)$

$\vec{F}_f = -5.1 \text{ N}$

5.) What would be the acceleration of the mass in #4 above given $\mu = 0.2$?

(1) $\vec{F}_{net} = \vec{F}_{||} + \vec{F}_f$ $\vec{F}_{net} = +14.715 + (+5.1)$ $\vec{F}_{net} = -9.61757$

(2) $\vec{F}_{net} = m \vec{a}$ $-9.61 = (3.0)(\vec{a})$ $\vec{a} = -3.21 \text{ m/s}^2$

Answers

- 1.) -245 N 2.) $-3.45 \frac{m}{s^2}$ 3.) +19.6 N, \vec{F}_n 1.) 0 N 2.) +500 N 3.) +600 N 4.) $+3.12 \frac{m}{s^2}$ at 50° N of E 5.) 16.9 N at 14° N of W
 1.) 0.26 2.) 2.19 kg 3.) linear, μ 1.) 0.245 m 2.) $+9800 \frac{N}{m}$
 1.) $\vec{F}_n = +37.5 \text{ N}$ $\vec{F}_{down} = -31.5 \text{ N}$ 2.) $+4.9 \frac{m}{s^2}$ 3.) +25.5 N 4.) -5.09 N 5.) $+3.20 \frac{m}{s^2}$